

1. Which of the following apply to why the lump sum formula holds?

- we used each short-term compounding period (local) to build upon and derive a global formula for the total savings plus interest
 - we took a process that originally had too many terms (one for each compounding period)
 - we reduced it to something manageable by finding the commonality of multiply by $(1 + \text{rate})$ and applying the algebra of exponents
 - this class is intended to be “plug and chug” so we never derived the lump sum formula—it was presented as mathematical magic
- a) all but the last statement
- b) only the last statement
- c) other

2. If a certificate of deposit (c.d.) will be compounded monthly at 3% for 14 years, and William put in \$2000, then what is the formula that represents how much would the c.d. be worth at the end of 14 years?

a) $2000(1 + .03)^{14}$

b) $2000(1 + \frac{.03}{14})^{14 \times 12}$

c) $2000(1 + \frac{.03}{12})^{14 \times 12}$

d) $2000(1 + \frac{.03}{12})^{14}$

e) none of the above

3. If a certificate of deposit (c.d.) will compounded monthly at 3% for 14 months, and William put in \$2000, how much would the c.d. be worth at the end of 14 months (answer in dollars and cents)? **Caution:** the previous question asks about 14 years but this problem asks about 14 months.

- a) \$3025.18
- b) \$2865.55
- c) \$3042.33
- d) \$2071.15
- e) none of the above

An exclusive conversation with Warren Buffett—PBS

Oct 3, 2008

https://www.youtube.com/watch?v=ejIWp5E8_Fo

- What is the problem with Americans keeping their money under their mattress?
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total = principal $(1 + \text{periodic rate})^{\text{number of times we actually compound}}$
application of algebra of factoring $(1 + \text{rate})$
application of algebra of exponents

What is the *interest* when \$37 is deposited today into an account that earns 12.99% compounded monthly for 2 years?

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$$37\left(1 + \frac{.1299}{12}\right)^{24}$$

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$$37\left(1 + \frac{.1299}{12}\right)^{24} - 37 = \$10.91$$

Futurama: A Fishful of Dollars

Bank Teller: *Ok. You had a balance of 93 cents... and at an average of two and a quarter percent interest [compounded annually] over a period of 1000 years, that comes to...*

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4.3 billion dollars

Futurama: A Fishful of Dollars

$$.93(1 + .0225)^{1000}$$

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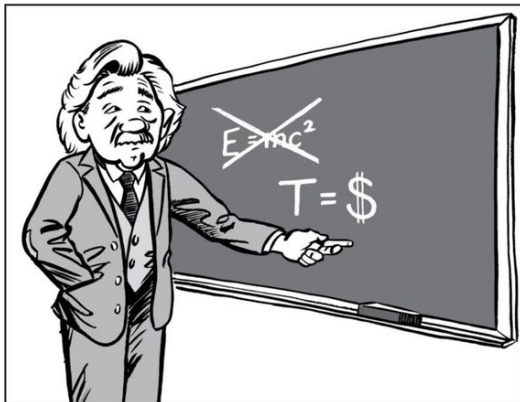
Futurama: A Fishful of Dollars

$$.93(1 + .0225)^{1000} \approx \$4,283,508,449.71$$

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Actually it was Benjamin Franklin

INVESTMENT BANKER MAN



It turns out Einstein really discovered that time is money

Image Credit: Rob Slee <https://twitter.com/timereallymoney/status/655419400124833794>

Lisa's Thrifty Savers savings account in Bart the Fink

Lisa put in \$100 for one year into a Thrifty Savers 2.3% savings account instead of a 2.25% account, and she earned an extra nickel. What equation represents this scenario?

$$.05 =$$

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$$.05 = 100\left(1 + \frac{.023}{n}\right)^n - 100\left(1 + \frac{.0225}{n}\right)^n$$

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Benjamin Franklin's Financial Legacy

- time, rate, number of times compounded, human element
- lump sum is appropriate
- average earned rate
- Goal seek, Microsoft Excel
- real-life history



1. Hypothetical Situation: If the fund lent out half of its money at 5% to borrowers who all paid back their loans plus interest, but if the fund could not find any borrowers for the other half of the money (i.e. 0%), what would the average earned rate of the fund be (take the weighted average—half at 5% and half at 0%—your response is a rate, not a dollar amount)?

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2. The fund lent some of its money to borrowers who didn't repay anything. How would that “rate” contribute in the calculation of the average earned rate?
Circle one: negative 0 positive

ASULearn Engagement

- Our Constitution is in actual operation; everything appears to promise that it will last; but in this world nothing is certain but death and taxes.
 - Benjamin Franklin, Polymath and Founding Father
- It would be a hard government that should tax its people one-tenth part of their income.
 - Benjamin Franklin, *Poor Richard's Almanac*, 1758
- The only difference between a tax man and a taxidermist is that the taxidermist leaves the skin.
 - Mark Twain, Writer
- America is a land of taxation that was founded to avoid taxation.
 - Dr. Laurence J. Peter, Educator
- I like to pay taxes. It is purchasing civilization.
 - Oliver Wendell Holmes, United States Supreme Court Justice
- This [preparing my tax return] is too difficult for a mathematician. It takes a philosopher.
 - Albert Einstein, Theoretical Physicist