

7.4 Partial Fractions (Quotients of Polynomials)

- Useful when denominator of quotient of polynomials and divides up into real factors that are linear or irreducible quadratic (or repeated)
- Based on adding fractions via a common denominator to make it easier to integrate

$$\frac{2}{x-2} + \frac{3}{x+1} \quad \leftarrow ? \quad \frac{5x-4}{x^2-x-2}$$

Partial Fractions

Factor

$$(ax + b)$$

$$(ax + b)^2$$

$$(ax^2 + bx + c)$$

Term in Partial Fraction Decomposition

$$\frac{A}{ax+b} + \frac{B}{(ax+b)^2}$$
$$\frac{Ax+B}{ax^2+bx+c}$$

7.4 Trig Substitution

Use if you see any algebraic expression that looks like the Pythagorean theorem (i.e., $\sqrt{a^2 - x^2}$ or $\sqrt{x^2 + a^2}$) but regular w -sub fails.

- Identify what trig sub to use ($x = a \sin \theta$, $x = a \tan \theta$).
- Write x and dx .
- Sketch the triangle with the sides filled in.
- Convert the integral to one with only θ .
- Simplify the radical using algebra and/or the pic...

