

7.4 Partial Fractions

Group Work Target Practice

Work in groups of two or three.

1. For $\frac{2}{s^4 - 1}$ write out the factors and the generic forms for the partial fractions and numerators, but **do not solve** for the constants. (Hint: In partial fractions, each linear factor (including any repeated linear terms) gets a constant as the numerator, and each irreducible quadratic gets a linear numerator, so you'll have a sum of terms like $\frac{A}{s + 1}$)

2. Solve for $\int \frac{3x + 11}{x^2 - x - 6} dx$ using the method of partial fractions. Show work.

Factor the denominator into linear and irreducible quadratic terms: $x^2 - x - 6 =$

Write the generic forms for the partial fractions and numerators:

$$\frac{3x + 11}{x^2 - x - 6} =$$

Multiply through by the common denominator and expand:

$$3x + 11 =$$

Create equations using like terms:

x terms:

constant terms:

Now you have a linear system of 2 equations and 2 unknowns. Solve this linear system for A, B and show work.

Write out the integral as the sum of the partial fraction integrals, and then compute it. If you are feeling comfortable with w -substitution then in this specific context you do not need to write out the substitution details.

$$\int \frac{3x + 11}{x^2 - x - 6} dx =$$