### 8.2 Volume of Surface of Revolutions

1. Sketch a graph of the object you want to find the volume of
2. What axis are you revolving about?
3. Slice perpendicular to this axis of revolution. Sketch a picture of a Riemann slice on your graph.
4. Which is the infinitesimal part of the slice? Circle: $\Delta x$ or $\Delta y$
5. Is the slice a solid cylindrical region or an annular/washer region?

If it is a solid region, what is $r$ in terms of the integration variable?
If it is an annular region, what is $r_{\text {outer }}$ ? What is $r_{\text {inner }}$ in terms of this variable?
6. What is the Riemann sum approximation? $\sum$
7. What is $a$ and $b$ ? Write the integral?

Common forms: $\int_{a}^{b} \pi r^{2} d x$ or $\int_{a}^{b} \pi\left(r_{\text {outer }}^{2}-r_{\text {inner }}^{2}\right) d x=\int_{a}^{b} \pi r_{\text {outer }}^{2} d x-\int_{a}^{b} \pi r_{\text {inner }}^{2} d x$

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