1. Which of the following statements about are true about the

nullspace (or null space) and column space of $M = \begin{bmatrix} 1 & 4 \\ 2 & 5 \\ 3 & 6 \end{bmatrix}$.

Note that M is row equivalent to $M = \begin{bmatrix} 1 & 4 \\ 0 & -3 \\ 0 & 0 \end{bmatrix}$ and when M is

augmented with a generic vector and reduced to Gaussian, the last row becomes $\begin{bmatrix} 0 & 0 & b_1 - 2b_2 + b_3 \end{bmatrix}$

a) The column space is the plane $b_1 - 2b_2 + b_3 = 0$ in \mathbb{R}^3

b) The column space is the plane $s \begin{vmatrix} 1 \\ 2 \\ 3 \end{vmatrix} + t \begin{vmatrix} 4 \\ 5 \\ 6 \end{vmatrix}$ in \mathbb{R}^3

- c) The nullspace is the zero vector in \mathbb{R}^2
- d) more than one of the above, but not all of them
- e) all of a), b), and c)

2. If a matrix is not square, then the column space is a subspace of

- a) \mathbb{R} number of rows
- b) _ℝnumber of columns
- c) further work must be done to tell

HTMLJ The convex basis of the left null space of the stoichiometric matrix leads to the definition of metabolically meaningful pools I Famili, <u>BO Palsson</u> - Biophysical journal, 2003 - Elsevier

... between the reaction rate vectors, v, and time derivative of metabolite concentrations, dx/dt or

x^{*}. Each two subspaces in the domain (ie, the **null space** and row space) and codomain (ie, the left **null space** and **column space**) form orthogonal pairs with one another ...

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Closed-loop subspace identification using the parity space J Wang, SJ Qin - Automatica, 2006 - Elsevier

... It is shown that the column space of the observability matrix extracted from SOPIM is equivalent to that from SIMPCA-We...(9), we have (11) im N → ∞ 1 N (Γ f ⊥) T [I - H f] Z f Z p T = 0. Therefore, (Γ f ⊥) T [I - H f] is in the left null space of lim N → ∞ (1 / N) Z f Z p T . If we ...

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C Cornwell, P Schmidt, RC Sickles - Journal of econometrics, 1990 - Elsevier

... Let $PL_r = Q(Q'Q>Q')$ be the projection onto the column space of Q and $ML_r = I - Pp$ be the projection onto the **null space** of Q. We derive three different estimators for (2.3), each of which is a straight-forward extension of an established procedure for the standard panel data ...

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N Lee, JB Lim, J Chun - IEEE Transactions on Information ..., 2010 - ieeexplore.ieee.org

... designed to lie in the **null space** of channel matrix, ie ... Since all users have antennas and the relay equips antennas, there exists a -dimensional intersection subspace constil-tuted by the column space of channel matrices for each user pair. Let denote the ...

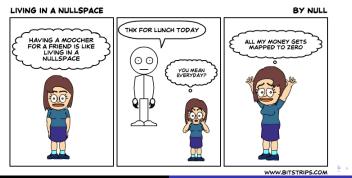
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3. The definition of a basis is a linearly independent spanning set for V. Which of the following also describes a basis?

- a) A basis is a minimal spanning set for V
- b) A basis is a largest possible set of linearly independent vectors in *V*
- c) An efficient way (linearly independent) to represent a space (span) linearly
- d) all of the above
- e) two of the above



Dr. Sarah

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