What do you see when you look at this matrix?
$\left[\begin{array}{lll}1 & 4 & 7 \\ 2 & 5 & 8 \\ 3 & 6 & 9\end{array}\right]$

- intersection of the rows for concurrent solutions of systems of equations
- mixing of the columns in vector equations for to check span and linear independence
- arrays as stand alone entities with their own algebra like associativity but not commutativity.
elementary row operations are matrix multiplications on the left $E A$.
function perspectives in 1.8, 1.9, 2.7
arrays transform objects or space: A linear transformation $T$

1. $T(\vec{x}+\vec{y})=T(\vec{x})+T(\vec{y})$
2. $T(c \vec{x})=c T(\vec{x})$
function perspectives in 1.8, 1.9, 2.7
arrays transform objects or space: A linear transformation $T$

$$
\begin{aligned}
& \text { 1. } T(\vec{x}+\vec{y})=T(\vec{x})+T(\vec{y}) \\
& \text { 2. } T(c \vec{x})=c T(\vec{x})
\end{aligned}
$$

left multiplication: Even though multiplication is not commutative, what makes it so useful is that linear transformations function as (left) matrix multiplication.
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- Hill cipher acts on the left of the code as multiplication by the coding matrix
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- $A$ invertible transforms in ways that can be undone, without a loss of information
- $A$ not invertible like $T: \mathbb{R}^{2} \rightarrow \mathbb{R}^{2}$ via $T(\vec{x})=A \vec{x}$ where

$$
\begin{aligned}
& A=\left[\begin{array}{ll}
0 & 0 \\
0 & 0
\end{array}\right] . \\
& {\left[\begin{array}{ll}
0 & 0 \\
0 & 0
\end{array}\right]\left[\begin{array}{l}
x \\
y
\end{array}\right]=}
\end{aligned}
$$

smushes objects and spaces and is not recoverable

