What do you see when you look at this matrix?

- intersection of the rows for concurrent solutions of systems of equations
- mixing of the columns in vector equations for to check span and linear independence
- arrays as stand alone entities with their own algebra like associativity but not commutativity.

elementary row operations are matrix multiplications on the left *EA*.

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arrays transform objects or space: A linear transformation T

1. 
$$T(\vec{x} + \vec{y}) = T(\vec{x}) + T(\vec{y})$$

 $2. T(c\vec{x}) = cT(\vec{x})$ 

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  - A not invertible like  $T: \mathbb{R}^2 \to \mathbb{R}^2$  via  $T(\vec{x}) = A\vec{x}$  where

$$A = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}.$$
$$\begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} =$$
smushes objects and spaces and is not recoverable