## Axiomatic Systems, Measurement, and Constructions

- straightedge and compass
- paper folding-isometries of the plane (linear transformations that preserve length)
- Interactive Geometry Software (IGS) move geometric figure-configuration like the skeletal system of the human body or a mechanical device with interconnected parts, levers, and linkages-preserves dependency relationships to reveal invariants



## Euclid's Elements

CC BY-SA 3.0 Euclid's Elements 1573 Edition. Private collection Hector Zenil.


## Euclid's Elements Postulates


https://www.storyofmathematics.com/hellenistic_euclid.html

## Euclid's Elements I-1

I-1: On a given finite straight line, to construct an equilateral triangle (with only straightedge, compass, and intersection)


Let $\overline{A B}$ be a line segment. We'll construct an equilateral triangle with $\overline{A B}$ as the base...

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paper folding:
https://www.youtube.com/watch?v=6dA2R8bLb7Q

## Propositions, Assumptions and Applications

 Proof Considerations: I can write rigorous proofs in geometry, identify underlying assumptions, and understand limitations and applications.

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equilateral triangles are stable, inherently rigid, examples? pool table, methane molecule

## Euclid's Elements I-11

I-11: To draw a straight line at right angles to a given straight line from a given point on it (with only straightedge, compass, and intersection)

https://i.redd.it/xu89vcweusc11.jpg
Purr-pendicular directly used in I-13, I-46, and I-48

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Purr-pendicular directly used in $\mathrm{I}-13, \mathrm{I}-46$, and $\mathrm{I}-48$ engineering, construction, road intersections, Snell's law, Voronoi diagrams, normal force, principal component analysis

## Where is North?



I keep having a recurring nightmare where I am trapped in the following axiom system:

- A1: Coyotes and roadrunners live on the surface of a perfectly round planet.
- A2: Coyotes only begin chasing roadrunners exactly 2 seconds after the roadrunner passes them.
- A3: Coyotes can only catch roadrunners if they can catch up to them after having chased them.
- A4: Roadrunners run faster than coyotes.
- A5: Coyotes stop chasing roadrunners when they disappear from view.
- A6: All coyotes have 20/20 vision.

Will I be able to catch the roadrunner? If needed, can you add other axioms to the system, which are consistent with A1 through A6, that will ensure that I will always catch the roadrunner? Help me - you're my only hope! Hungry as ever, Wile E. Coyote

## Euclid's Elements I-10

To bisect a given finite straight line.


