

- Think about a possible answer(s), discuss your thoughts with your neighbors, and respond on

[pollev.com/drsarah314](http://pollev.com/drsarah314)

Which of the following is  $\alpha'(s)$  where  $s$  is the arc length parameter?

- a) velocity
  - b) unit tangent vector  $T$
  - c) curvature
  - d) more than one answer works
  - e) none of the above
- Prepare to share from your group's discussion. This may take the form of an assertion, question, definition, example, or other connection. It could also be something you tried and rejected.
  - May be a lag at times—review related concepts and examples, add to your notes, or get to know each other!

How did chain rule arise in the arc length  $s$ ,  $T$ , velocity, speed, acceleration and jerk interactive video?

- a) In the prior video on the tractrix, it was a part of the computation of the arc length of the tractrix as it was needed for the velocity and hence speed, and we used that again in this video
- b) It arose in the proof that every differentiable curve that is regular can be reparameterized by arc length
- c) When we are computing  $T(t)$  instead of  $T(s)$ , it's chain rule at work!
- d) all of the above
- e) exactly two of the above

## Arc Length $s$ and Unit Tangent $T$ of Helix

Work with neighbors or check-in with them regularly:

$\alpha(t) = (a \cos(t), a \sin(t), bt)$  where  $a, b \in \mathbb{R}$  constants

- Compute unit tangent  $T(t) = \frac{\alpha'(t)}{|\alpha'(t)|}$
- Compute arc length  $s(t) = \int_0^t |\alpha'(u)| du$
- Write the inverse function  $t(s)$  by solving for  $t$
- Reparameterize the curve by arc length  $\beta(s) = \alpha(t(s))$



<http://previews.123rf.com/images/limbi007/limbi0071302/limbi007130200034/>

17726502-Orange-cartoon-characters-runs-on-the-green-helix-Stock-Photo-orange-spiral

# Differential Geometry of Helix in Maple

- velocity, acceleration, jerk
- speed and arc length
- $T$  in Frenet-Serret TNB Frame, curvature and torsion



<http://previews.123rf.com/images/limbi007/limbi0071302/limbi007130200034/>

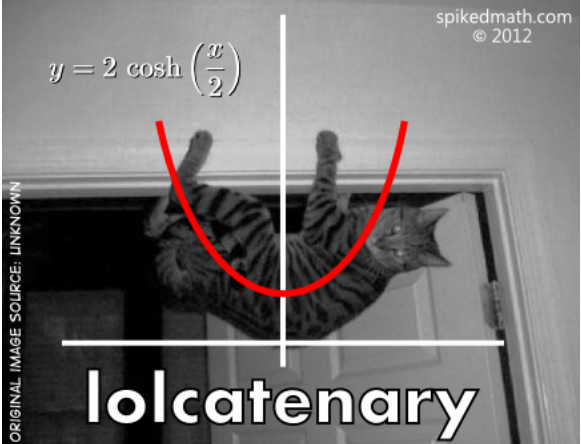
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$$y = 2 \cosh\left(\frac{x}{2}\right)$$

ORIGINAL IMAGE SOURCE: LINKDOWN



# lolcatenary

In physics and geometry, the lolcatenary is the curve that an idealized hanging lolcat assumes under its own weight when supported only at its ends.