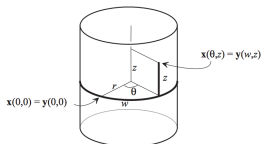
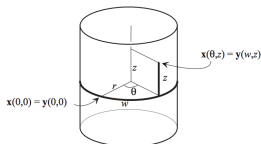


Coordinates on a Cylinder



- Choose $(0,0,0)$, and $3 \perp$ axes
- Choose $+z$ as a cylinder height axis
- Let θ be the angle traveled from the origin in the xy plane

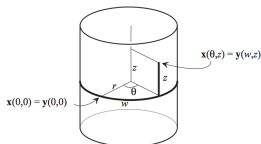
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Extrinsic coordinates : $x(\theta, z) = (r\cos(\theta), r\sin(\theta), z)$

Coordinates on a Cylinder

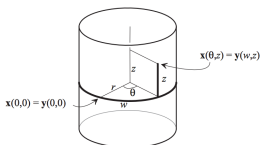


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Problem: Bug no awareness of 3-space

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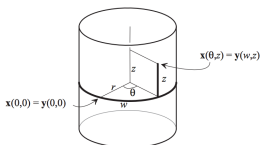
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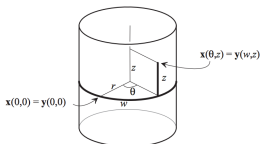
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Problem: Bug no awareness of 3-space

- Choose $(0,0)$ as an intrinsic origin. There is 1 geodesic that will return there, so call that the base curve

Coordinates on a Cylinder



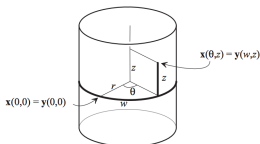
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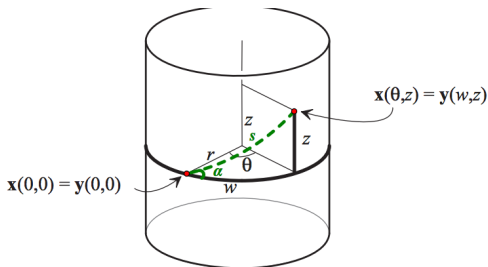
Problem: Bug no awareness of 3-space

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- Choose $+z$ as a direction \perp to the base curve

Intrinsic coordinates (geodesic rectangular coordinates) :

$y(w, z) =$ walk w units along base curve and turn 90 degrees to positive z -direction and travel z units.

Coordinates on a Cylinder



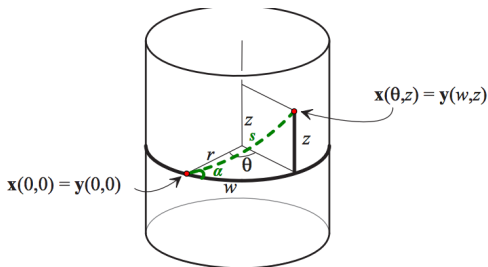
Extrinsic coordinates: $x(\theta, z) = (r\cos(\theta), r\sin(\theta), z)$

Equation of cylinder: $x^2 + y^2 = r^2$ in \mathbb{R}^3

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Intrinsic coordinates:

Geodesic rectangular coordinates: $y(w, z) =$ walk w units along base curve and turn 90 degrees to positive z -direction and travel z units.

Geodesic polar coordinates: $y(\alpha, s) =$ turn α degrees from the base curve and walk s units along that geodesic