Review of Material for Differential Geometry

Review **definitions**, **big picture ideas**, **visualizations**, **and examples**. During class we'll briefly review 2130 and 2240 concepts as they naturally arise in differential geometry over the course of the semester. Solidifying any material you aren't feeling comfortable with before and after we cover it will also help you solidify the related differential geometry concepts.

Ideas from the pre-requisite multivariable calculus: Calculus and Analytic Geometry III is a pre-requisite for the class, and we'll be building off the following topics, so it will be helpful to review to make sure you understand the concepts and know how to do a computational example.

- 1. equation of a line in 3-space
- 2. tangent line
- 3. equation of a plane
- 4. tangent plane
- 5. parametrizations of curves and surfaces
- 6. velocity and acceleration
- 7. speed
- 8. tangent vector
- 9. normal vector
- 10. tangential and normal components of acceleration
- 11. curvature
- 12. arc length
- 13. surface area
- 14. volume
- 15. cylindrical and spherical coordinates
- 16. derivative of a function of one variable whose range is in \mathbb{R}^3 , i.e. (x(t), y(t), z(t))
- 17. partial derivatives of a multivariable function i.e. f(x,y)
- 18. multivariable chain rule
- 19. gradient
- 20. Green's Theorem
- 21. Stokes' Theorem
- 22. directional derivative
- 23. fundamental theorem of calculus
- 24. dot product
- 25. cross product
- 26. norm or length of a vector
- 27. derivative of dot product of two vectors

Ideas from co-requisite linear algebra: If you have taken Introduction to Linear already, it would be helpful to review the following concepts, and if not, it would be helpful to pay special attention as these concepts come up in 2240 and in differential geometry:

- 1. matrix notation a_{ij}
- 2. multiplication of matrices
- 3. inverse of a 2x2 matrix
- 4. addition of matrices
- 5. transpose of a matrix
- 6. determinant of a matrix
- 7. symmetric matrix
- 8. linear combination of vectors
- 9. span of vectors
- 10. basis of a space
- 11. dimension of a space
- 12. eigenvalue