

1.  $f(x) : \mathbb{R} \rightarrow \mathbb{R}$  is continuous at  $x_0$  if
  - a)  $\exists \epsilon > 0, \text{ s.t. } \forall \delta > 0 \text{ and } \forall x, |x - x_0| < \delta \Rightarrow |f(x) - f(x_0)| < \epsilon$
  - b)  $\forall \epsilon > 0, \exists \delta > 0 \text{ s.t. } \forall x, |x - x_0| < \delta \Rightarrow |f(x) - f(x_0)| < \epsilon$
  - c)  $\forall \epsilon > 0, \exists \delta > 0 \text{ s.t. } \forall x, d'(x, x_0) < \delta \Rightarrow d'(f(x), f(x_0)) < \epsilon$
  - d) All of the above
  - e) More than one answer from a, b and c holds, but not all three
  
2. Which of the following hold?
  - a)  $f(C_1 \cap C_2) = f(C_1) \cap f(C_2)$
  - b)  $f(C_1 \cup C_2) = f(C_1) \cup f(C_2)$
  - c)  $f(C_1 \cap C_2) \subseteq f(C_1) \cap f(C_2)$
  - d) Only a) and b)
  - e) Only b) and c)
  - f) Only a) and c)
  
3. Which of the following are open sets?
  - a) An open interval in  $\mathbb{R}$
  - b) An open diamond in  $\mathbb{R}^2$
  - c) An open diamond in  $\mathbb{R}_{\text{taxicab}}^2$
  - d) Only a) and b)
  - e) Only a) and c)
  - f) All of the above: a), b) and c)
  
4. In a successful proof that  $B_d(x, \epsilon)$  is open, if  $y \in B_d(x, \epsilon)$ , what  $\delta$  can you take for  $B_d(y, \delta)$  to be in  $B_d(x, \epsilon)$ ?
  - a) Take  $\delta = \epsilon$
  - b) Take  $\delta = \epsilon - d(x, y)$
  - c) Take  $\delta = d(x, y) - \epsilon$
  - d) Any of the above are possible
  - e) It is not possible to choose a  $\delta$  successfully because the set is not open
  
5. What sets are open in the discrete metric on X?
  - a) No sets are open
  - b) Only circles of radius 1 are open
  - c) Any subset of X is open
  - d) Other