

### **The Fibonacci Sequence**

The Fibonacci sequence consists of  $\{0, 1, 1, 2, 3, 5, 8, 13, \dots\}$ . After looking at this sequence for a moment one can easily see that beginning with the third element, each element is the sum of the two preceding elements. This can be notated by,

$$Y_{k+2} = Y_{k+1} + Y_k \text{ where } k = 0, 1, 2, \dots$$

$Y_{k+2}$  depends on the function  $F$ , where  $F(k, Y_{k+1}, Y_k) = Y_{k+1} + Y_k$  which depends on  $k$ .

$$Y_{k+2} = F(k, Y_{k+1}, Y_k) = F(k, Y_{k+1}, Y_k).$$

Therefore,  $Y_{k+2} = Y_{k+1} + Y_k$  forms the rule for the sequence.