Work quickly and carefully, following directions closely. Answer all questions completely.

FOR ALL PROBLEMS: Define P, Q, R, and S to be the four digits in your given number.

$$P = \underline{\hspace{1cm}}, \qquad Q = \underline{\hspace{1cm}}, \qquad R = \underline{\hspace{1cm}}, \qquad S = \underline{\hspace{1cm}}.$$

- §I. TRUE and/or FALSE. Circle your answer. There are 2 questions at 2 points each.
  - 1. TRUE or FALSE: The Laplace transform of a periodic function is also periodic.
  - 2. TRUE or FALSE: The *Laplace transform* of the function  $y = Pe^{(x^2+Q)}$  does not exist. (*P* and *Q* are your numbers.)
- §II. MULTIPLE CHOICE. Circle your answer. There are 2 question at 5 points each.
  - 1. The *Laplace transform* of the *shifted Dirac Delta function*  $\delta(t-R)$  (where *R* is your number) is

(a) 
$$F(s) = e^{-Rs}$$
 (b)  $F(s) = \frac{e^{-Rs}}{s}$  (c)  $F(s) = se^{-Rs}$  (d) none of the above

2. The *inverse Laplace transform* of  $F(s) = \frac{Ps}{P^2 + s^2}$  (where P is your number) is

(a) 
$$f(t) = \frac{1}{2}t^{-1}\sin(Pt)$$
 (b)  $f(t) = \frac{1}{2}\sin(Pt)$  (c)  $f(t) = \frac{1}{2}t\sin(Pt)$  (d) none of the above

- §III. PROBLEMS. You must show your work to receive credit. There are 3 problems at 10 points each.
  - 1. Find the *Laplace transform* of the function  $f(t) = e^{-Qt} \sin(t)$ . (*Q* is your number.)

FOR ALL PROBLEMS: Define P, Q, R, and S to be the four digits in your given number.

$$P = \underline{\hspace{1cm}}, \qquad Q = \underline{\hspace{1cm}}, \qquad R = \underline{\hspace{1cm}}, \qquad S = \underline{\hspace{1cm}}.$$

2. Find the *inverse Laplace transform* of the function  $F(s) = \frac{P}{s^2 - Ps}$ . (*P* is your number.)

3. Solve the differential equation  $x''(t) + x(t) = \delta(t - Q)$  with x(0) = 0 and x'(0) = 0. (Q is your number.)