

Problem 7e, pg 257.

with(*LinearAlgebra*) :

$$A := \begin{bmatrix} 1 & 3 & 2 & 1 \\ 4 & 2 & 1 & 2 \\ 2 & 1 & 2 & 3 \\ 1 & 2 & 4 & 1 \end{bmatrix} :$$

$$b := \langle -2, 2, 1, -1 \rangle$$

$$b := \begin{bmatrix} -2 \\ 2 \\ 1 \\ -1 \end{bmatrix} \tag{1.1}$$

GaussianElimination($\langle A | b \rangle$)

$$\begin{bmatrix} 1 & 3 & 2 & 1 & -2 \\ 0 & -10 & -7 & -2 & 10 \\ 0 & 0 & \frac{3}{2} & 2 & 0 \\ 0 & 0 & 0 & -\frac{17}{5} & 0 \end{bmatrix} \tag{1.2}$$

$x_{soln} := \text{BackwardSubstitute}(\mathbf{(1.2)})$

$$x_{soln} := \begin{bmatrix} 1 \\ -1 \\ 0 \\ 0 \end{bmatrix} \tag{1.3}$$

$A \cdot x_{soln} = b$

$$\begin{bmatrix} -2 \\ 2 \\ 1 \\ -1 \end{bmatrix} = \begin{bmatrix} -2 \\ 2 \\ 1 \\ -1 \end{bmatrix} \tag{1.4}$$

Old package

`linalg[ffgausselim](⟨A|b⟩)`

$$\begin{bmatrix} 1 & 3 & 2 & 1 & -2 \\ 0 & -5 & -2 & 1 & 5 \\ 0 & 0 & 15 & 20 & 0 \\ 0 & 0 & 0 & -51 & 0 \end{bmatrix}$$

(2.1)

`linalg[backsub](%)`

$$\begin{bmatrix} 1 & -1 & 0 & 0 \end{bmatrix}$$

(2.2)