

with(LinearAlgebra):

A1 := << 1, 0 > | < 1, 2 >>

$$\begin{bmatrix} 1 & 1 \\ 0 & 2 \end{bmatrix} \quad (1)$$

A2 := << 1, 1 > | < 2, 0 >>

$$\begin{bmatrix} 1 & 2 \\ 1 & 0 \end{bmatrix} \quad (2)$$

A := DiagonalMatrix([A1, A2])

$$\begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 2 & 0 & 0 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 1 & 0 \end{bmatrix} \quad (3)$$

e := Eigenvectors(A, output=list)

$$\left[ \left[ \left[ \begin{array}{c} 1 \\ 0 \\ 0 \\ 0 \end{array} \right] \right], \left[ \begin{array}{c} 1 \\ 1 \end{array} \right], \left[ \left[ \begin{array}{c} 0 \\ 0 \\ -1 \\ 1 \end{array} \right] \right], \left[ \begin{array}{c} -1 \\ 1 \end{array} \right], \left[ \left[ \begin{array}{c} 1 \\ 0 \\ 0 \\ 1 \end{array} \right], \left[ \begin{array}{c} 0 \\ 0 \\ 2 \\ 1 \end{array} \right] \right], \left[ \begin{array}{c} 2 \\ 2 \end{array} \right] \right] \quad (4)$$

e||(1..4) := e[1, 3, 1], e[2, 3, 1], e[3, 3, 1], e[3, 3, 2]

$$\left[ \begin{array}{c} 1 \\ 0 \\ 0 \\ 0 \end{array} \right], \left[ \begin{array}{c} 0 \\ 0 \\ -1 \\ 1 \end{array} \right], \left[ \begin{array}{c} 1 \\ 1 \\ 0 \\ 0 \end{array} \right], \left[ \begin{array}{c} 0 \\ 0 \\ 2 \\ 1 \end{array} \right] \quad (5)$$

P := Matrix([e||(1..4)])

$$\begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & -1 & 0 & 2 \\ 0 & 1 & 0 & 1 \end{bmatrix} \quad (6)$$

Ap := P<sup>(-1)</sup>.A.P

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 2 & 0 \\ 0 & 0 & 0 & 2 \end{bmatrix} \quad (7)$$