

Homework:

Monday, Jan 10, 2011

§4.5; pg. 176, No. 4, 5, 7, 8, 12, 18, 26, 49.

Label each statement as true or false. If a statement is true, prove it. If not,

- (i) give an example of why it is false, and
- (ii) if possible, correct it to make it true, and then prove it.

4. A function f is continuous at $x = a$ if and only if $\lim_{x \rightarrow a} f(x) = f(a)$.

5. The function $f(x) = (1 - 2^{1/x})^{-1}$ has a jump discontinuity at $x = 0$.

7. Functions $f(x) = \sin(x)$ and $g(x) = \cos(x)$ are uniformly continuous on \mathbb{R} .

8. If a function f is uniformly continuous on every bounded interval, then f is uniformly continuous on \mathbb{R} .

12. If a function $f : D \rightarrow \mathbb{R}$ with $D \subseteq \mathbb{R}$ is continuous and the sequence $\{x_n\}$ is Cauchy in D , then $\{f(x_n)\}$ is Cauchy.

18. A function f exists that is uniformly continuous on (a, ∞) and for which $\lim_{x \rightarrow \infty} f(x) = \infty$.

26. The function $f(x) = \begin{cases} x \sin(\frac{1}{x}) & \text{if } x \text{ is rational} \\ 0 & \text{if } x \text{ is irrational} \end{cases}$ is continuous at the origin.

49. A composition of two continuous functions is continuous.