

goals:

Worksheet on Spherical Perspectives

Dr. Sarah's MAT 3610: Introduction to Geometry

- IGS Exploration

I can use Interactive Geometry Software (IGS) to discover relationships and demonstrate they seem to apply in a wide variety of examples.

- Proof Considerations

I can write rigorous proofs in geometry, identify underlying assumptions, and understand limitations and applications.

- Geometric Perspectives

I can compare and contrast multiple geometric perspectives.

Welcoming Environment: Keep it a safe place to express meaningful ideas and opinions. Actively listen to others and encourage everyone to participate. Part of the welcoming environment is to keep an open mind as you engage in our class activities, explore consensus and employ collective thinking across barriers. Maintain a professional tone, show respect and courtesy, and make your contributions matter.

1. **Building Community:** What are the preferred first names of those sitting near you? If you weren't able to be there write N/A or give reference to anyone you had help from.

Euclid's Postulates on the Sphere

2. Given two points A and B on the surface of a ball, what is the intrinsically straight path between them, the path that a toy car would take without turning its steering wheel, masking tape would follow without buckling, or string pulled tightly would fall on? These aren't extrinsically straight from the point of view of someone outside the ball, but they are intrinsically straight for those living on the space.
3. Read Euclid's Postulate 1. By using your last response as the intrinsically straight lines on the sphere—we have symmetry that could satisfy Definition 4's "lies evenly with the points on itself"—sketch 2 points A and B on the sphere, and an intrinsically straight line between them, demonstrating axiom 1.
4. Read Euclid's Postulate 2. Can we continue along straight lines on the sphere, wrapping back around as needed?
5. Euclid's Postulate 3: Use the string, with its length as the radius and start from a point P (perhaps the north pole) to look at the set of points equidistant from P . What would the circle of center P and radius the string length look like? Include a sketch of the sphere, the point, and the circle.

13. If not, identify the first underlying assumption from the proof that fails and explain.

Proposition 4: SAS Revisited

14. Using Euclid's definition of intrinsically straight paths—but not necessarily shortest distance paths—sketch two spherical triangles that satisfy the conditions of SAS on the sphere but are not congruent. The unusual one was in the Euclidean and spherical perspectives interactive video.

15. Review the Euclidean proof of SAS (*I* – 4) from the congruence and similarity 1 interactive video notes you took. In the video we looked at some underlying assumptions and limitations of the Euclidean proof. Where does the Euclidean proof of SAS first go wrong? Explain.

16. Reword Postulate 1 so that the underlying assumption that is used in the proof of *I* – 4 is explicitly stated.

17. **Help each other and PDF responses to ASULearn:** If you are finished with the worksheet before I bring us back together, first ensure that your entire group is finished too, and if not, help each other. If your entire group is finished, then split up and pull up chairs so that you can discuss your responses with other groups. Collate your handwritten responses, preferably on this handout, into one full size multipage PDF for submission in the ASULearn assignment. I recommend you turn it in sometime today, but you have until the next class.