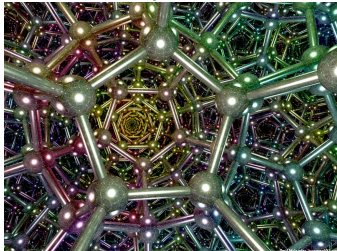
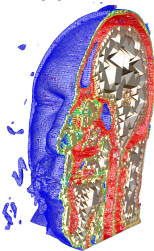
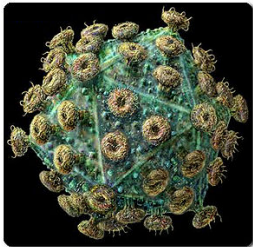


# Measuring Curvature at a Vertex

Structure of Viruses    Approximations    Shape of Universe



1. Russell Knightley. <http://www.rkm.com.au/VIRUS/HIV>, 2. K. Weiss & L. De Florian: Isodiamond Hierarchies, IEEE Transactions on Vis & Comp Graphics <http://kennyweiss.com/> 3. Paul Nylander: life from

<sup>the inside</sup>  
**Angle defect at a vertex** =  $360^\circ - \text{sum angles at a vertex}$

Polyhedron	Angle Defect	V (# Vertices)	Total Angle Defect
Dodecahedron			
flat soccer ball (truncated icosahedron)			

## *Why is the Total Angle Defect $720^\circ$ ?*

angle defect at a vertex =  $2\pi$  – sum angles at a vertex

total angle defect =

$$\sum_V \text{angle defect at a vertex} =$$

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sum of angles in 1 face =  $\pi(\# \text{ sides in face} - 2) = \pi(\# \text{ sides}) - 2\pi$

sum of all the angles =

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$\sum_V$  angle defect at a vertex =  $2\pi V$  – **sum of all the angles**

sum of angles in 1 face =  $\pi(\# \text{ sides in face} - 2) = \pi(\# \text{ sides}) - 2\pi$

**sum of all the angles** =  $\sum_F$  sum in each face =  $\pi$  (all sides) –  $2\pi F$ .

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total angle defect =

$$\sum_V \text{angle defect at a vertex} = 2\pi V - \text{sum of all the angles}$$

sum of angles in 1 face =  $\pi(\# \text{ sides in face} - 2) = \pi(\# \text{ sides}) - 2\pi$

$$\text{sum of all the angles} = \sum_F \text{sum in each face} = \pi(\text{all sides}) - 2\pi F.$$

Recall that all the sides double counts along the edges  $E$  so

$$\text{sum of all the angles} = 2\pi E - 2\pi F$$

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Recall that all the sides double counts along the edges  $E$  so

sum of all the angles =  $2\pi E - 2\pi F$

total angle defect =  $2\pi V - (2\pi E - 2\pi F) = 2\pi(V - E + F)$   
geometric combinatorics

## Polyhedra

In the proof that there are five regular polyhedra, recall that we had  $n$  total polygonal faces and  $p$   $k$ -sided faces touch at a vertex. Characterize  $E$  and  $V$  in terms of  $n, p$  and  $k$ .

a)  $E = \frac{nk}{2}$        $V = \frac{nk}{p}$

b)  $E = \frac{nk}{2}$        $V = \frac{nk}{2}$

c)  $E = \frac{nk}{p}$        $V = \frac{nk}{2}$

d)  $E = \frac{nk}{p}$        $V = \frac{nk}{p}$

e) other



## *Taxicab Geometry*

In taxicab geometry, do 3 noncollinear points determine a unique taxicab circle?

- a) yes and I have a good reason why
- b) yes but I am unsure of why
- c) no but I am unsure of why not
- d) no and I have a good reason why not
- e) other